

# Antiferromagnetic phase transition in garnet-type AgCa2Co2V3O12 and AgCa2Ni2V3O12

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# Antiferromagnetic phase transition in garnet-type AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>

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#### Abstract

Antiferromagnetic phase transition in two vanadium garnets  $AgCa_2Co_2V_3O_{12}$ and  $AgCa_2Ni_2V_3O_{12}$  has been found and investigated extensively. The heat capacity exhibits sharp peak due to the antiferromagnetic order with the Néel temperature  $T_N = 6.39$  K for  $AgCa_2Co_2V_3O_{12}$  and 7.21 K for  $AgCa_2Ni_2V_3O_{12}$ , respectively. The magnetic susceptibility exhibit broad maximum, and these  $T_N$  correspond to the inflection points of the magnetic susceptibility  $\chi a$  little lower than  $T(\chi_{max})$ . The magnetic entropy changes from zero to 20 K per mol Co<sup>2+</sup> and Ni<sup>2+</sup> ions are 5.31 J K<sup>-1</sup>mol-Co<sup>2+</sup>-ion<sup>-1</sup> and 6.85 J K<sup>-1</sup> mol-Ni<sup>2+</sup>-ion<sup>-1</sup>, indicating S = 1/2 for Co<sup>2+</sup> ion and S=1 for Ni<sup>2+</sup> ion. The magnetic susceptibility of  $AgCa_2Ni_2V_3O_{12}$  shows the Curie-Weiss behavior between 20 and 350 K with the effective magnetic moment  $\mu_{eff} = 3.23 \ \mu_B \ Ni^2$ -ion<sup>-1</sup> and the Weiss constant  $\theta = -16.4 \ K$ . The simple Curie-Weiss law can not be applicable for  $AgCa_2Co_2V_3O_{12}$ . The complex temperature dependence of magnetic susceptibility has been interpreted within the framework of Tanabe-Sugano energy diagram, which is analyzed on the basis of crystalline electric field. The ground state is the spin doublet state <sup>2</sup>E ( $t_2^6 e$ ) and the first excited state is spin quartet state  ${}^{4}T_1(t_2^5e^2)$  which locates extremely close to the ground state. The low spin state S = 1/2 for Co<sup>2+</sup> ion is verified experimentally at least below 20 K which is in agreement with the result of the heat capacity.

*Keywords:* A. Inorganic compounds; A. Oxides; D. Magnetic properties; D. Crystal fields; D. Specific heat

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#### 1. Introduction

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The garnet-type compounds have been attracting great interests on the magnetic properties in the theory and experiments, in particular, ferrimagnetism of rare earth iron garnets  $R_3$ Fe<sub>5</sub>O<sub>12</sub>[1]. Fig. 1 shows the garnet structure has cubic symmetry with space group *Ia*<sup>3</sup>d (No. 230). The general chemical formula of the oxide garnet may be written as  $\{C\}_{3}[A]_{2}(D)_{3}O_{12}$ , where C, A, and D-sites are the cation sites. These cation sites are surrounded by oxygen ions O<sup>2-</sup> at dodecahedron, octahedron, and tetrahedron, respectively. Many investigafor tions have been made the garnets with magnetic ions distributed over C, A, D-three or two sublattices. Garnets having only one magnetic sublattice are diluted magnetic system and are of interest as a simpler system.

When the *D*-site is occupied by  $V^{5^{\ddagger}}$  ion, so called vanadium garnet (V-garnet), many works were made mainly by Russian researches nearly 30 years ago [2-13], where detailed analysis has not been presented for the magnetic properties. These V-garnets can provide the diluted magnetic system or non-magnetic system. The V-garnets of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> are synthesized by Ronniger *et al.* [9], where only the lattice constants are given. No physical property has been measured so far.

We have also successfully synthesized high purity V-garnets of  $AgCa_2Co_2V_3O_{12}$ and  $AgCa_2Ni_2V_3O_{12}$  and  $AgCa_2Zn_2V_3O_{12}$ , where  $AgCa_2Zn_2V_3O_{12}$  is non-magnetic and then used as a standard compounds without magnetic properties. In these compounds, ionic distributions are  $\{AgCa_2\}[Co_2](V_3)O_{12}$  and  $\{AgCa_2\}[Ni_2](V_3)O_{12}$  and  $\{AgCa_2\}[Zn_2](V_3)O_{12}$ .

Ag<sup>+</sup> and Ca<sup>2+</sup> ions occupy C-site, Co<sup>2+</sup>, Ni<sup>2+</sup> or Zn<sup>2+</sup> ions occupy A-site and V<sup>5+</sup> ions occupy D-site. Here these Co<sup>2+</sup> and Ni<sup>2+</sup> ions at A-site are only magnetic and the other ions have closed shell with non-magnetic state. The studies of the synthesis and crystallographic refinement by the Rietveld method for  $AgCa_2Co_2V_3O_{12}$  and  $AgCa_2Ni_2V_3O_{12}$  have been published in our previous report [14]. We have measured the heat capacity and the magnetic susceptibility of V-garnets. The antiferromagnetic Néel order have first found with  $T_{\rm N} = 6.39$  K for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and 7.21 K for AgCa<sub>2</sub>NI<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. In antiferromagnetic ordered state addition. the has not been observed The down to 4.2 Κ for  $AgCa_2Cu_2V_3O_{12}$ [15]. Néel temperature could be below 1 K. In this paper, the experimental results of thermal and magnetic proper-

 $AgCa_2Ni_2V_3O_{12}$ 

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 $AgCa_2Co_2V_3O_{12}$ 

tails within the frame work of Tanabe-Sugano energy diagram. The particular emphasis and attention are paid to the significant difference between Co<sup>2+</sup> and Ni2+ ions at octahedron A-site under the influence of crystalline electric field (CEF). The free ions of  $\operatorname{Co}^{2+}(3d^7)$  and  $\operatorname{Ni}^{2+}(3d^8)$  ions have an orbital F state (L = 3)as ground state. For Co<sup>2+</sup> ion, there remains Kramer's degeneracy, therefore the correlation between CEF and the spin-orbit interaction is more complicated in comparison with  $Ni^{2+}$  ion system. This paper will present the difference of the magnetic state between  $AgCa_2$   $Co_2(V_3)O_{12}$  and  $AgCa_2$   $Ni_2(V_3)O_{12}$  and will provided. The magnetic susceptibility of AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> shows the Curie-Weiss behavior between 20 and 350 K with the effective magnetic moment  $\mu_{eff} = 3.23 \ \mu_{\rm B} \ {\rm Ni}^{2+}$ -ion<sup>-1</sup>. The magnetic susceptibility result of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> shows the complex temperature dependence. We discuss this result on the basis of the idea that the excited state influences significantly the magnetic susceptibilthe presence thermally accessible high-spin itv. arising from of а state lying above the low-spin ground state. The knowledge of CEF enables us to understand the complex temperature dependence of the magnetic susceptibility for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub>, which will be discussed below.

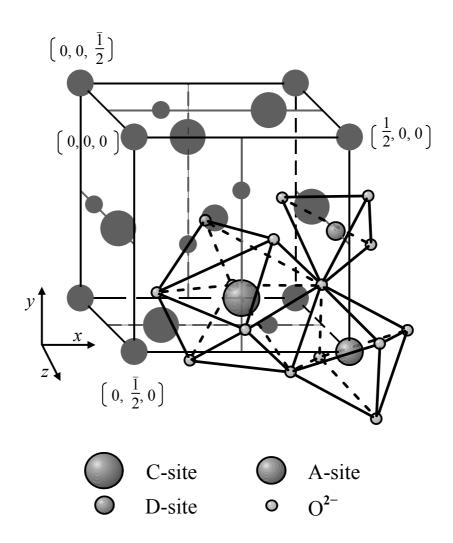


Fig. 1. An eighth of unit cell of garnet-type structure  $\{C\}_3[A]_2(D)_3O_{12}$  with the different sites *C*, *A* and *D*.

#### 2. Experimental methods

Powder specimens of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub>, AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub> were prepared through a solid-state chemical reaction. The synthesis and detailed crystallographic studies of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> have been recently made on the basis of the Rietveld analysis in which the refined structure parameters are presented [14]. The synthesis and magnetic property studies of AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub> have been published on ref. [15]. The heat capacity was measured with a Quantum Design PPMS Heat Capacity Option (HC) Model P650 over the temperature range 0.42 to 60 K in zero field. The dc magnetic susceptibility  $\chi$  of powder specimen was measured with a Quantum Design superconducting quantum interference device (MPMS, *rf*-SQUID) magnetometer over the temperature range 2.0 to 350 K under zero field cooled (ZFC) and field cooled (FC) conditions.

### 3. Results and discussion

#### 3.1 *Heat capacity*

#### 3.1.1 Lattice heat capacity

Fig. 2 depicts the molar (formula-unit) heat capacity *C* as a function of temperature over the range 0.42 to 40 K. Two compounds of  $AgCa_2Co_2V_3O_{12}$  and  $AgCa_2Ni_2V_3O_{12}$  exhibit a sharp peak due to the antiferromagnetic phase transition at 6.39 K and 7.21 K, respectively.

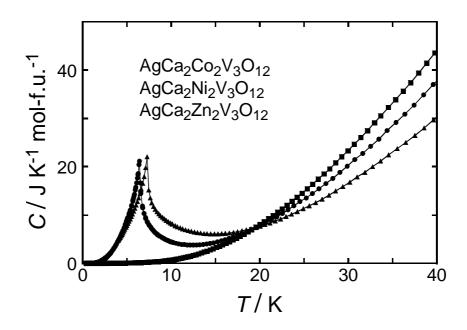


Fig. 2. Measured heat capacity of vanadium garnets as a function of the temperature.

On the other hand  $AgCa_2Zn_2V_3O_{12}$  is non-magnetic and then C does not indimagnetic anomaly lattice heat cate any but only the capacity The magnitude heat of the capacity in Fig.  $C_{\text{lattice}}$ . 2 for three compounds is fairly same around 20 K and the experimental values grow rapidly above 20 K. It is noted that the molar weights are 650.71 g mol^-1 for  $AgCa_2Co_2V_3O_{12}$ , 650.23 g mol^-1 for  $AgCa_2Ni_2V_3O_{12}$  and 663.66 g mol<sup>-1</sup> for  $AgCa_2Zn_2V_3O_{12}$ ; the order of the value of  $C_{lattice}$  for three compounds is reasonable. The curve of  $AgCa_2Zn_2V_3O_{12}$  in Fig. 2 shows  $C_{lattice}$ , following the Debye  $T^3$  approximation.

$$C_{\text{lattice}} = \left(\frac{12}{5}\right) \pi^4 N_A k_B r \left(\frac{T}{\Theta_D}\right)^3$$

$$= 1943.8 r \left(\frac{T}{\Theta_D}\right)^3$$
(1)

- 4 -

where  $N_A$  is the Abogadro's number,  $k_B$  the Boltzmann's constant,  $\Theta_D$  the Debye temperature, *T* the temperature and *r* the number of atoms per formula unit, which is found to be r =20 for garnet compound. Fig. 3 is the Debye *T*<sup>3</sup> approximation of low temperature lattice heat capacity for AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub> as a function of the temperature. The Debye temperature  $\Theta_D$  is obtained to be 410 K (r = 20) and 151 K (r = 1).

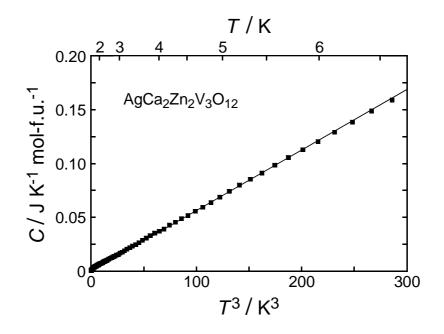


Fig. 3. The Debye  $T^3$  approximation of low temperature lattice heat capacity for AgCa<sub>2</sub>Zn<sub>2</sub>V<sub>3</sub>O<sub>12</sub>.

The accurate subtraction of the lattice contribution from the total heat capacity of  $AgCa_2Co_2V_3O_{12}$  and  $AgCa_2Ni_2V_3O_{12}$  is a rather serious problem. Here we subtracted  $C_{\text{lattice}}$  by using the experimental value of the  $AgCa_2Zn_2V_3O_{12}$ . Furthermore we adopt ed the molecular mass correction using the following relation,

$$C'_{\text{lattice}} = \left(\frac{M'}{M}\right)^{\frac{3}{2}} C_{\text{lattice}}, \qquad (2)$$

where  $C_{\text{lattice}}$  is the lattice heat capacity of  $\text{AgCa}_2\text{Zn}_2\text{V}_3\text{O}_{12}$ , and the  $C'_{\text{lattice}}$  is the hypothesized lattice heat capacity of  $\text{AgCa}_2\text{Co}_2\text{V}_3\text{O}_{12}$  or  $\text{AgCa}_2\text{Ni}_2\text{V}_3\text{O}_{12}$ , as if these  $\text{AgCa}_2\text{Co}_2\text{V}_3\text{O}_{12}$ and  $\text{AgCa}_2\text{Ni}_2\text{V}_3\text{O}_{12}$  would be just non-magnetic compounds. The values of  $(M'/M)^{3/2}$ are  $9.71 \times 10^{-1}$  for  $\text{AgCa}_2\text{Co}_2\text{V}_3\text{O}_{12}$  and  $9.70 \times 10^{-1}$  for  $\text{AgCa}_2\text{Ni}_2\text{V}_3\text{O}_{12}$ .

#### **3.1.2** Nuclear Zeeman effect of the heat capacity for cobalt nucleus

The experimental value of the heat capacity for  $AgCa_2Co_2V_3O_{12}$  exhibits the slight increase with decreasing temperature below 0.7 K, while this increase was not found in the heat capacity of  $AgCa_2Ni_2V_3O_{12}$  at low temperature. In Fig. 4, the solid circles show the heat capacity of  $AgCa_2Co_2V_3O_{12}$  after the subtraction of the lattice contribution. We presume this increase of the heat capacity of  $AgCa_2Co_2V_3O_{12}$  indicates the tail of the nuclear spin heat capacity  $C_{nuclear}$  due to the nuclear Zeeman effect of Co nucleus with I = 7/2. The nuclear spin I = 7/2 of <sup>59</sup>Co has 100 % natural abundance, while <sup>61</sup>Ni nucleus has I = 3/2 but low 1.1399 % natural abundance and therefore negligibly small effect. Therefore, Co nucleus with I = 7/2 is influenced strongly by the internal field due to the electron moment arisen from the antiferromagnetic order of  $Co^{2+}$  ion below  $T_N = 6.39$  K. In the temperature range 0.42 to 0.49 K, C versus  $1/T^2$  plot follows in a straight line, where C indicates the heat capacity after the subtraction of  $C_{lattice}$ .

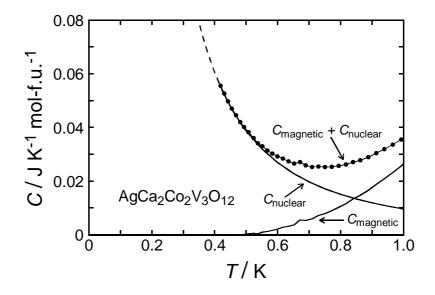


Fig. 4. The expanded plot of the low temperature heat capacity of  $AgCa_2Co_2V_3O_{12}$  after the subtraction of lattice contribution. The nuclear Zeeman effect heat capacity for Co nucleus and magnetic heat capacity for  $Co^{2+}$  ion are overlapped. Here, the magnetic heat capacity of  $Co^{2+}$  ion is calculated from the value of experimental result minus nuclear Zeeman effect, see text.

Fig. 4 represents the expanded plot of low temperature heat capacity of  $AgCa_2Co_2V_3O_{12}$  which consists of two parts with  $C_{nuclear}$  and the magnetic heat capacity  $C_{magnetic}$  originated from  $Co^{2+}$  ion. The solid curve of  $C_{nuclear}$  indicates the extrapolated result assuming  $1/T^2$  form and the  $C_{magnetic}$  indicates calculated results of  $C - C_{nuclear}$ .

Let us calculate the nuclear Zeeman heat capacity under the internal magnetic field due to the  $Co^{2+}$  ion. The partition function Z of the nuclear Zeeman split for Co nucleus with I = 7/2 is

$$Z = \sum_{j} g_{j} \exp\left(-\frac{\varepsilon_{j}}{k_{\rm B}T}\right) = 2\sum_{j=1}^{4} \cosh\left(\frac{2j-1}{2}\frac{\varDelta}{k_{\rm B}T}\right),\tag{3}$$

where  $g_j$  is the degree of degeneracy,  $\varepsilon_j$  the energy,  $\Delta$  the difference between the each energy level, here the origin of the energy is assumed to be the center of width of the Zeeman splitting. The internal energy U is

$$U = \frac{N}{Z} \sum_{j} \varepsilon_{j} \exp\left(-\frac{\varepsilon_{j}}{k_{\rm B}T}\right)$$
$$= -\frac{\Delta N}{Z} \sum_{j=1}^{4} (2j-1) \sinh\left(\frac{2j-1}{2}\frac{\Delta}{k_{\rm B}T}\right),$$
(4)

where N is the number of magnetic ions. The nuclear spin Zeeman heat capacity at constant volume of Co nucleus is given by,

$$C_{\text{nuclear}} = \left(\frac{\partial U}{\partial T}\right)_{\text{v}} ,$$

$$= \left(\frac{\Delta}{k_{\text{B}}T}\right)^{2} \frac{Nk_{\text{B}}}{Z^{2}} (A - B) ,$$

$$A = \left\{\sum_{j=1}^{4} (2j - 1)^{2} \cosh\left(\frac{2j - 1}{2} \frac{\Delta}{k_{\text{B}}T}\right)\right\} \left\{\sum_{j=1}^{4} \cosh\left(\frac{2j - 1}{2} \frac{\Delta}{k_{\text{B}}T}\right)\right\}$$

$$B = \left\{\sum_{j=1}^{4} 2(2j - 1) \sinh\left(\frac{2j - 1}{2} \frac{\Delta}{k_{\text{B}}T}\right)\right\} \left\{\sum_{j=1}^{4} \frac{2j - 1}{2} \sinh\left(\frac{2j - 1}{2} \frac{\Delta}{k_{\text{B}}T}\right)\right\} .$$
(5)

The asymptotic form of  $C_{\text{nuclear}}$  at higher temperature is obtained in terms of  $1/T^2$  as  $k_{\rm B}T >> \Delta$ ,

$$C_{\text{nuclear}} \approx \frac{21}{4} \left( \frac{\Delta}{k_{\text{B}}T} \right)^2 N k_{\text{B}} \qquad \left( k_{\text{B}}T >> \Delta \right).$$
 (6)

The value  $\Delta$  is estimated to be 5.17 tesla (10.6 mK, 1.46 × 10<sup>-25</sup> J) in comparison - 7 -

with the formula (6) and the experimental result. Fig. 5 shows the calculated result of the heat capacity due to the nuclear Zeeman effect of Co nucleus in  $AgCa_2Co_2V_3O_{12}$ . The peak is 10.8 mK, and maximum value of  $C_{nuclear}$  is about 15.0 J K<sup>-1</sup> mol-f.u.<sup>-1</sup>.

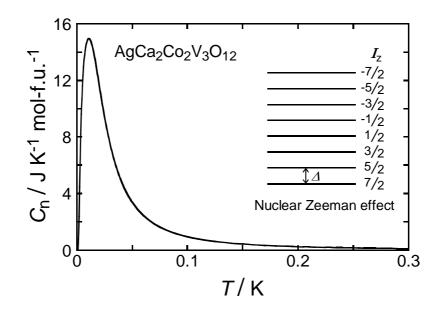


Fig. 5. Nuclear Zeeman effect of  $Co^{2+}$  ion in AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. Nuclear spin heat capacity as a function of the temperature at low temperature.

#### 3.1.3 Antiferromagnetic heat capacity

Fig. 6 shows the temperature dependence of the magnetic heat capacity  $C_{\text{magnetic}}$  of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> coming from the electron spin. These magnetic heat capacities are obtained after the subtraction;  $C_{\text{magnetic}} = C - C_{\text{lattice}} - C_{\text{nucclear}}$  for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and  $C_{\text{magnetic}} = C - C_{\text{lattice}}$  for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>, where *C* indicates the total heat capacity measured experimentally. The sharp peak corresponds to the Néel temperature  $T_{\text{N}}$  which is 6.39 K for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and 7.21 K for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. Fig. 7 displays the magnetic heat capacity in the narrow temperature region over 4.0 to 9.0 K around  $T_{\text{N}}$ . The magnetic enthalpy  $E_{\text{magnetic}}$  is evaluated by

$$E_{\text{magnetic}} = \int_{0}^{T} C_{\text{magnetic}} dT \quad . \tag{7}$$

The values of  $E_{\text{magnetic}}$  over the temperature range zero to 20 K are 34.9 J mol-Co<sup>2+</sup>-ion<sup>-1</sup> for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and 50.9 J mol-Ni<sup>2+</sup>-ion<sup>-1</sup> for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>.

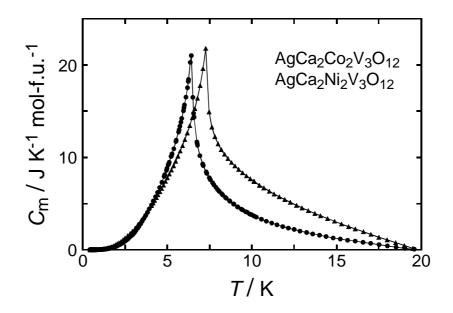


Fig. 6. Magnetic heat capacity of  $AgCa_2Co_2V_3O_{12}$  and  $AgCa_2Ni_2V_3O_{12}$  a function of the temperature. The Néel temperature is 6.39 K for  $AgCa_2Co_2V_3O_{12}$  and 7.21 K for  $AgCa_2Ni_2V_3O_{12}$ .

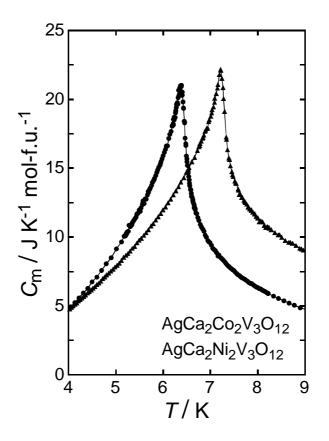


Fig. 7. The expanded plot of the magnetic heat capacity around the Néel temperature.

Fig. 8 indicates the temperature dependence of  $C_{\text{magnetic}}/T$  for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. The experimental observation of the magnetic entropy change  $S_{\text{magnetic}}$ over the temperature range zero to 20 K is presented in Fig. 9 using the following expression,

$$S_{\text{magnetic}} = \int_0^T \frac{C_{\text{magnetic}}}{T} \, dT \, . \tag{8}$$

Fig. 9 depicts the magnetic entropy  $S_{\text{magnetic}}$ /mol-magnetic-ion of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> as a function of the temperature. The total magnetic entropy change  $\Delta S_{\text{magnetic}}$ /mol-magnetic-ion is 5.31 J K<sup>-1</sup> mol-Co<sup>2+</sup>-ion<sup>-1</sup> for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and 6.85 J K<sup>-1</sup> mol-Ni<sup>2+</sup>-ion<sup>-1</sup> for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. The calculated entropy change  $\Delta S_{\text{magn$  $netic}}$ /mol-ion is 5.76, 9.13 and 11.5 J K<sup>-1</sup> mol-ion<sup>-1</sup>, for the value of spin S = 1/2, 1 and 3/2; further, the values in the unit of  $\Delta S_{\text{magnetic}}/R = \ln(2S + 1)$  per mol-ion are 0.693, 1.10 and 1.39, respectively, R is the gas constant. It is stressed that the experimental result of entropy change supports the spin value of S = 1/2 for Co<sup>2+</sup> ion in AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. As for Ni<sup>2+</sup> ion in AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>, the experimental value is a little less than that of expected value for S= 1, where the origin of this difference may come from the overestimation of the lattice heat capacity. The ratio of the magnetic entropy change below and above  $T_{\text{N}}$ is evaluated to be  $\Delta S_{\text{magnetic}}(T < T_{\text{N}}) = 58$  % and  $\Delta S_{\text{magnetic}}(T > T_{\text{N}}) = 42$  % for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub>;  $\Delta S_{\text{magnetic}}(T < T_{\text{N}}) = 60$  % and  $\Delta S_{\text{magnetic}}(T > T_{\text{N}}) = 40$  % for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>.

The A-site sublattice consists of bcc structure where the magnetic interactions between each magnetic ion are fairly complicated. It should be noticed that the strong short-range order (SRO) effect has been observed in these two garnets of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. Figs. 6 and 7 show the not  $\lambda$ -type anomaly of the heat capacity but rather symmetrical shape between below and above  $T_N$  in narrow temperature region, which is one of the typical characteristics of low-dimensional magnetic phase transition. Fig. 9 also demonstrates the SRO effect which indicates that the magnetic entropy change above  $T_{\rm N}$  is approximately 40 % for both garnets. The magnetic ions at A-site are separated in series by at least two O2- ions from the nearest neighbor magnetic one. The magnetic interaction is rather novel. As a consequence the theory of superexchange coupling interaction can not be applicable to understand these V-garnet systems. The determination of the magnetic structure is great significant, which will be the coming issue of these compounds. The substantial amount of magnetic dipole-dipole interaction may be not completely neglected in this system because the number of the nearest neighbor of magnetic ion is 8 and next n.n. is 6. The spin wave excitation of the three-dimensional antiferromagnetic system predicts  $T^3$  law of  $C_{\text{magnetic}}$  at low temperature. Figs. 10 and 11 show a  $T^3$  plots of  $C_{\text{magnetic}}$  for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. The experimental data is fairly in agreement with the theoretical prediction of  $T^3$  law over the temperature range 0.42 to 5.85 K for  $AgCa_2Co_2V_3O_{12}$  and 0.42 to 3.27 K for  $AgCa_2Ni_2V_3O_{12}$ . long-range Once these compounds undergo the order on passing below  $T_{\rm N}$ , the three-dimensional interaction is established firmly and then the spin wave excitation of the three-dimensional antiferromagnetic system with  $T^3$  law can be expected.

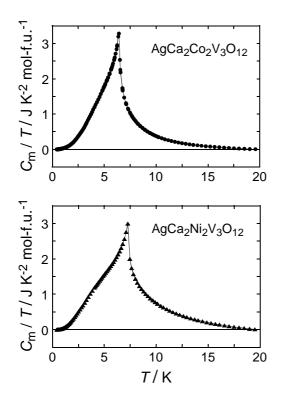


Fig. 8.  $C_{\text{magnetic}}/T$  versus T plots for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>.

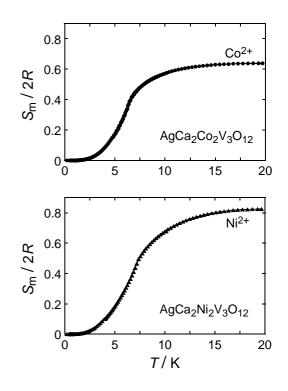


Fig. 9. Magnetic entropy of  $AgCa_2Co_2V_3O_{12}$ and  $AgCa_2Ni_2V_3O_{12}$  as a function of the temperature. The unit of the vertical axis is defined to be magnetic entropy per mol-magnetic-ion.

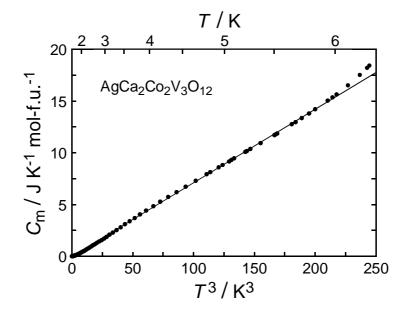


Fig. 10. Magnetic heat capacity versus  $T^{3}$  for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> on the basis of antiferromagnetic spin wave excitation.

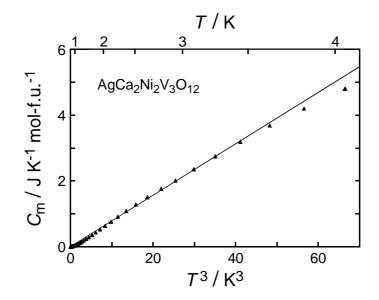


Fig. 11. Magnetic heat capacity versus  $T^3$  for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> on the basis of antiferromagnetic spin wave excitation.

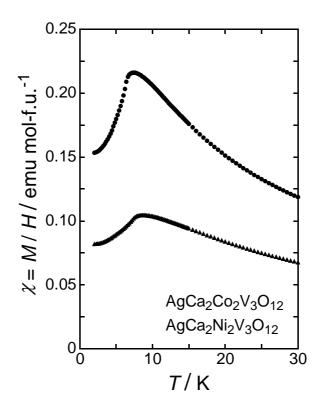


Fig. 12. Magnetic susceptibilities  $\chi$  for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> as a function of temperature, obtained in an applied field of 1.00 kOe under zero-field cooled condition.

#### 3.2 Magnetic susceptibility

# 3.2.1 $AgCa_2Ni_2V_3O_{12}$

Fig 12 shows the temperature dependence of the magnetic susceptibility  $\chi$  in an applied field *H* of 1.00 kOe for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. The susceptibility is caused by localized magnetic moment of Co<sup>2+</sup> ion and Ni<sup>2+</sup> ion and has antiferromagnetic order with round maximum of  $\chi_{max}$  with the temperatures of 7.40 K and 8.80 K, respectively. The values of  $\chi(2.0 \text{ K})/\chi_{max}$  are 0.71 for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and 0.78 for AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> which are a little larger than 2/3 expected for antiferromagnets for the powder specimen. Fig. 13 presents the temperature derivative of  $\chi$  as a function of the temperature. This peak temperature of  $d\chi/dT$  corresponds to that at the sharp peak of the heat capacity, defining the Néel temperature. It is noted that the temperature of round maximum of  $\chi_{max}$  is not in agreement with  $T_N$  observed in the heat capacity.

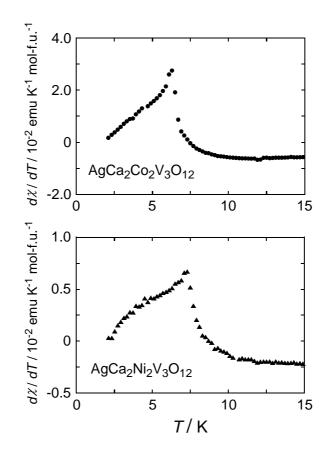


Fig. 13. Temperature derivative of  $\chi$  as a function of temperature, using the data of Fig. 12. This peak temperature of  $d\chi/dT$  corresponds to that at the sharp peak of the heat capacity, indicating Néel temperature.

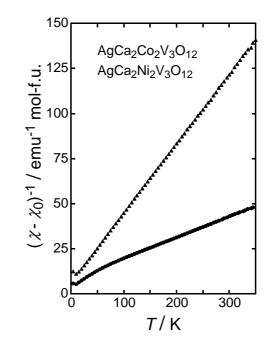


Fig. 14. Inverse magnetic susceptibility as a function of temperature in a constant magnetic field of 10.0 kOe. The solid circle shows  $AgCa_2Co_2V_3O_{12}$  and the solid triangle shows  $AgCa_2Ni_2V_3O_{12}$ .

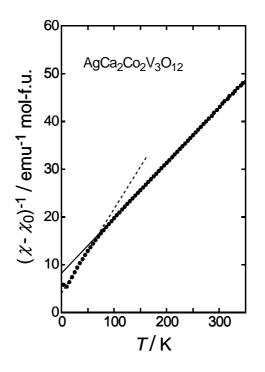


Fig. 15. The expanded plot of the inverse susceptibility in a constant magnetic field of 10.0 kOe for  $AgCa_2Co_2V_3O_{12}$ . The solid line shows a fit over the high temperature range 100 to 350 K and the dotted line shows the lower temperature region 20 to 60 K.

The inverse magnetic susceptibility in an applied magnetic field H of 10.0 kOe is indicated in Fig. 14. The susceptibility of AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> is well described over the temperature range 20 to 350 K by a modified Curie-Weiss law,

$$\chi = \frac{C}{T - \theta} + \chi_0, \tag{9}$$

where *C* is the Curie constant,  $\theta$  the Curie-Weiss  $\theta$  and  $\chi_0$  a temperature independent term, *T* the temperature. The experimental result of  $\chi_0$  is found to be  $3.16 \times 10^{-3}$  emu mol-f.u.<sup>-1</sup>. The amount of diamagnetic contribution caused by the atomic core electrons  $\chi_{\text{dia}}$  for Ag<sup>+</sup> + 2Ca<sup>2+</sup> + 2Ni<sup>2+</sup> + 3V<sup>5+</sup> + 12O<sup>2-</sup> is evaluated to be  $-2.18 \times 10^{-4}$  emu mol-f.u.<sup>-1</sup> [16]. The Curie-Weiss  $\theta$  is -16.4 K and about 2.27 times of  $T_{\rm N} = 7.21$  K. The magnitude of the effective magnetic moment  $\mu_{\rm eff}$  from the value of C = 2.60 K emu mol-f.u.<sup>-1</sup> is  $3.23 \ \mu_{\rm B} \ Ni^{2+}$ -ion<sup>-1</sup>, which is close to the spin only value 2.83  $\mu_{\rm B}$  expected for S = 1, where the Lande's g-factor might be expected to be 2.28.

# 3.2.2 $AgCa_2Co_2V_3O_{12}$

The paramagnetic susceptibility  $\chi$  of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> over the temperature range 20 to 350 K does not obey the Curie-Weiss law as shown in Figs. 14 and 15. The susceptibility  $\chi$  can not be described by one straight line over a wide temperature range. Here if we just pick up the experimental data for two temperature regions in Fig. 15, then we can obtain the fictitious (wrong) results as follows; (a)  $20 \le T \le 60$  K :  $\chi_0 = -2.95 \times 10^{-3}$  emu mol-f.u.<sup>-1</sup>,  $\theta = -23.0$  K, C = 5.68 K emu mol-f.u.<sup>-1</sup>, and  $\mu_{eff} = 4.77$   $\mu_{\rm B}$  Co<sup>2+</sup>-ion<sup>-1</sup>, (b)  $100 \le T \le 350$  K :  $\chi_0 = -2.95 \times 10^{-3}$  emu mol-f.u.<sup>-1</sup>,  $\theta = -71.3$  K, C = 8.66 K emu mol-f.u.<sup>-1</sup>, and  $\mu_{eff} = 5.88$   $\mu_{\rm B}$  Co<sup>2+</sup>-ion<sup>-1</sup>. The diamagnetic susceptibility by the atomic core orbital contribution  $\chi_{\rm dia}$  for Ag<sup>+</sup> + 2Ca<sup>2+</sup> + 2Co<sup>2+</sup> + 3V<sup>5+</sup> + 12O<sup>2-</sup> is estimated to be  $\chi_{\rm dia} = -2.20 \times 10^{-4}$  emu mol-f.u.<sup>-1</sup> [16]. There is experimental uncertainty in the  $\chi_0$  although the value itself is small.

At first sight, these experimental results for the susceptibility of  $AgCa_2Co_2V_3O_{12}$ may lead to an apparent interpretation that the high and low spin crossover takes place approximately 100 K where in the higher temperature  $\mu_{eff}$  is 5.88  $\mu_{p}$  while 4.77  $\mu_{p}$ in the lower temperature. However, it should be noted that these values of the effective magnetic moment  $\mu_{\text{eff}}$  are completely different from these magnitudes expected for 3.87  $\mu_{\text{B}}$  (S = 3/2 high spin state) and for 1.73  $\mu_{\rm B}$  (S = 1/2 low spin state). In addition, the magnitude of the antiferromagnetic Weiss temperature  $\theta = -71.3$  K is too high in comparison with  $T_{\rm N} = 6.39$  K. The simple understanding on the basis of the Curie-Weiss law should be rejected. Consequently this simple interpretation is wrong. The authors would like to point out careful understanding and discussion as follows. These results are discussed in conjunction with the outstanding Tanabe-Sugano energy diagram based on the cubic crystalline electric field theory with the octahedral symmetry [17, 18]. The unified physical picture has been derived from the same discussion reported in Ref. [19] within the framework of Tanabe-Sugano energy diagram. Here we present the significant energy levels only around the ground state shown in Fig. as 16. Tanabe-Sugano of which refers to the energy diagram ref. [17.] 18]. The crystalline electric field parameter Dq indicates the strength of CEF and B is Racah's parameter defined as the value of linear combination of Slater integrals introduced grals introduced by Racah [17, 18]. The transition from the weak CEF with high spin state to the strong CEF with low spin state takes place for  $Co^{2+}$  ion at the vertical line of Dq/B~2.17. The Rietveld analysis has been accomplished for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> [14]. The result tells interesting  $AgCa_2Co_2V_3O_{12}$ result that the  $CoO_6$ -octahedron of is firm and tight. The bond length between Co2+ and O2- is 2.087(4) Å, which is exshort tremely and sufficient to provide the strong CEF. Presumably the same strong CEF takes place in the AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub>.

Our experimental results may indicate that the value of Dq for AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> is located at the just after the transition of from high spin to low spin state. Here Dq/B is ~2.3 just a little larger than  $Dq/B \sim 2.17$ . This Tanabe-Sugano energy diagram for  $d^7$  configuration for Co<sup>2+</sup> at  $Dq/B \sim 2.3$  indicates that the energy level constructs from the ground state  ${}^{2}E(t_2{}^{6}e)$ at the bottom to  ${}^{4}T_1(t_2{}^{5}e^2)$ ,  ${}^{2}T_1$ ,  ${}^{2}T_2$ ,  ${}^{4}T_2(t_2{}^{4}e^3)$ ,  ${}^{4}T_1$ ,  ${}^{2}A_1$ ,  ${}^{4}A_2(t_2{}^{3}e^4)$ , and the highest state of  ${}^{2}A_2$ . On the other hand, the energy levels for the free ion of Co<sup>2+</sup> with Dq/B = 0 from the bottom ground state to the highest state are  ${}^{4}F$ ,  ${}^{4}P$ ,  ${}^{2}G$ ,  ${}^{2}H$ ,  ${}^{2}P$ ,  ${}^{2}_{a}D$ ,  ${}^{2}F$ , and  ${}^{2}_{b}D$ . In the influence of CEF,  ${}^{4}F$  ground state splits into  ${}^{4}T_1(t_2{}^{5}e^2)$ ,  ${}^{4}T_2(t_2{}^{4}e^3)$  and  ${}^{4}A_2(t_2{}^{3}e^4)$  and the second excited state  ${}^{2}G$  plays an important role because  ${}^{2}G$  state also splits under the influence of CEF. One of the split component of  ${}^{2}G$  state is  ${}^{2}E$  state which becomes the ground state in the strong CEF of value Dq/B larger than ~2.17. This  ${}^{2}E$  state crosses all the quartet levels on its way down, as can be seen in the Tanabe-Sugano energy diagram, see Fig. 16.

The magnitude of  $Dq/B \sim 2.3$  for  $AgCa_2Co_2V_3O_{12}$  gives two significant levels of the ground state  ${}^{2}E(t_2{}^{6}e)$  and the first excited state of  ${}^{4}T_1(t_2{}^{5}e^2)$ . The  ${}^{4}T_1(t_2{}^{5}e^2)$  state is extremely close to  ${}^{2}E(t_2{}^{6}e)$  state and a little higher than that. We can not neglect the thermally accessible occupation of the excited state  ${}^{4}T_1(t_2{}^{5}e^2)$  for the interpretation of the magnetic susceptibility.

Here let us take a next step. It is unable for us to pursue a quantitative analysis of the susceptibility because of the many unknown parameters in the crystalline electric field theory. Therefore we try a feasible approach where the basic view point from the Tanabe-Sugano energy diagram is maintained. We introduce an effective magnetic moment  $p_{\rm eff}$  which is expressed by [20],

$$p_{\rm eff} = \frac{1}{\mu_{\rm B}} \sqrt{\frac{3k_{\rm B}(\chi - \chi_0)T}{N}} , \qquad (10)$$

here  $\chi$  is the experimental value of the temperature dependent magnetic susceptibility,  $k_{\rm p}$  the Boltzmann's constant,  $\mu_{\rm p}$  the Bohr magneton and N the number of magnetic ion. Temperature dependence of  $p_{\rm eff}$  per magnetic ion is shown in Figs. 17 and 18. For AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>, Fig. 17 indicates the same values of  $\chi(T)$  as these obtained in Fig. 14 for a comparison. The straight and horizontal line is seen over the wide temperature range over 50 to 300 K in AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> as shown in Fig. 17, which supports the ap-Curie-Weiss law. Nevertheless,  $AgCa_2Co_2V_3O_{12}$ plicability of the demonstrates the curved line for  $p_{\rm eff}$  as seen in Fig. 18. We note that the measured value of  $\chi(T)$ includes the temperature independent Van Vleck paramagnetic contribution in addition to the stated diamagnetic core contribution  $\chi_0$  and/or appreciable experimental errors, then we must subtract before being compared with theoretical results. Fig. 18 shows the  $\chi_0$  dependence of  $p_{\rm eff}$  as a function of temperature. Any magnitude of  $\chi_0$ does not fulfill and reproduce a straight and horizontal line. The complex temperature dependence of the susceptibility is reflected in the performance of  $p_{eff}$ , which originates from the existence of the first excited spin quartet  ${}^{4}T_{1}(t_{2}{}^{5}e^{2})$  state just a bit higher than the ground spin doublet  ${}^{2}E(t_{2}{}^{6}e)$  state. Consequently two magnetic states with S = 3/2 and S = 1/2 are excited and active magnetically at higher temperature. It should be noticed that our model does not mean the simple high (S = 3/2) to low spin state (S = 1/2) transition, but the z-component  $S_{z}$  of spin is 6, because +1/2, -1/2 from ground state and +3/2, +1/2, -1/2, and -3/2, so that this value corresponds effectively (not exactly) to S = 5/2 where the presence of a thermally accessible spin 3/2 excited. The above analysis has been treated within the framework of the Tanabe-Sugano theory.

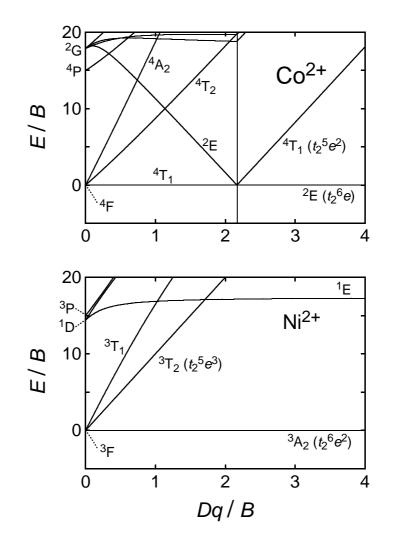


Fig. 16. The energy diagram close to the ground state which is referred to as the Tanabe-Sugano energy diagram based on the cubic crystalline electric field theory with the octahedral symmetry. The level energy (ordinate) is measured from the ground state and the strength of the crystalline electric field (abscissa) is scaled by B as unit, see text and Refs. [17,18].

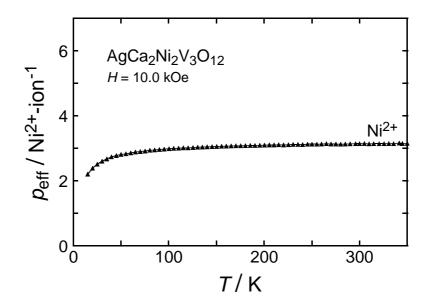


Fig. 17. The effective magneton number of Ni<sup>2+</sup> ion in AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub> as a function of temperature;  $\chi_0 = 3.16 \times 10^{-3}$  emu mol-f.u.<sup>-1</sup>.

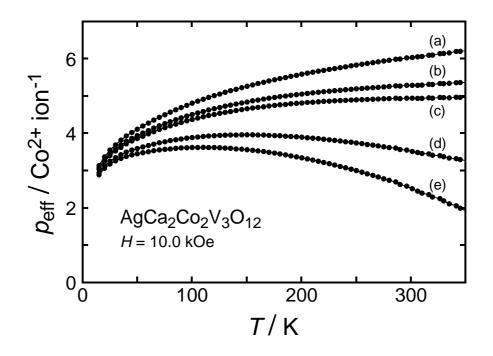


Fig. 18. The variation of the effective magneton number of Co<sup>2+</sup> ion in AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> on the magnitude of  $\chi_0$ : (a)  $\chi_0 = -1.00 \times 10^{-2}$ emu mol-f.u.<sup>-1</sup>, (b)  $\chi_0 = -2.95 \times 10^{-3}$  emu mol-f.u.<sup>-1</sup>, (c)  $\chi_0 = 0.00$ emu mol-f.u.<sup>-1</sup>, (d)  $\chi_0 = 1.00 \times 10^{-2}$  emu mol-f.u.<sup>-1</sup>, (e)  $\chi_0 = 1.50 \times 10^{-2}$ emu mol-f.u.<sup>-1</sup>.

It should be noted, nevertheless, that the other nice route to reach the Co<sup>2+</sup> problem in the octahedral field on the basis of the spin-orbit coupling [21], and the spin Hamiltonian method [22]. Here we have omitted the detailed discussion on the basis of these theories, see Ref. [19, 21, 22]. We point out that many previous researchers experienced a severe struggle for understanding the magnetic susceptibility for the almost same structure of vanadium garnet NaCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> [3, 5, 10] and NaPb<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> [19]. The garnet structure contains CoO<sub>6</sub> octahedron at the A-site of Co<sup>2+</sup> ion which has extremely rigid. Consequently, Co<sup>2+</sup> ion is strongly influenced by the CEF of O<sup>2-</sup> ions. These difficulty can be removed by the existence of excited spin quartet state  ${}^{4}T_{1}(t_{2}{}^{5}e^{2})$  just a little bit higher than ground spin doublet state  ${}^{2}E(t_{2}{}^{6}e)$  state, on the basis of CEF theory. Fig. 16 predicts also that the electron configuration  $d^{8}$  for Ni<sup>2+</sup> ion in the cubic CEF with octahedral symmetry does not cause the transition from high to low spin state when the CEF strength parameter Dq varies from weak to strong. The ground state of  $d^8$  for Ni<sup>2+</sup> ion in the cubic CEF maintains the spin triplet state  ${}^{3}A_{2}(t_{2}{}^{6}e^{2})$  with any changing the value of Dq, furthermore, the excited states of the energy levels in the cubic CEF are rather higher than that of the ground sate. Therefore the spin triplet state is fairly defined. These situation guarantees the applicability of the Curie-Weiss law to the magnetic susceptibility data of AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. Consequently, all the experimental results give the reasonable magnitudes expected.

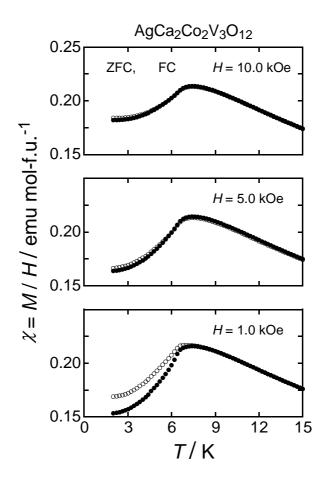


Fig. 19. Magnetic susceptibility of  $AgCa_2Co_2V_3O_{12}$  as a function of temperature in three magnetic fields of 10.000 kOe, 5.000 kOe and 1.000 kOe under ZFC and FC conditions.

## 3.2.3 Field dependence of the susceptibility below $T_{\rm N}$

Figs. 19 and 20 provide the magnetic field dependence magnetic susceptibility on emphasizing the temperature region below  $T_{\rm N}$ . The difference between field-cooled ( $\chi_{\rm FC} = M_{\rm FC}/H$ ) and zero-field-cooled ( $\chi_{\rm ZFC} = M_{\rm ZFC}/H$ ) susceptibility decreases with increasing field as can be seen in Figs. 19 and 20. This characteristic feature was found in both of AgCa<sub>2</sub>Co<sub>2</sub>V<sub>3</sub>O<sub>12</sub> and AgCa<sub>2</sub>Ni<sub>2</sub>V<sub>3</sub>O<sub>12</sub>. The deviation of  $\chi_{\rm FC}$  from  $\chi_{\rm ZFC}$  starts higher temperature with decreasing field.

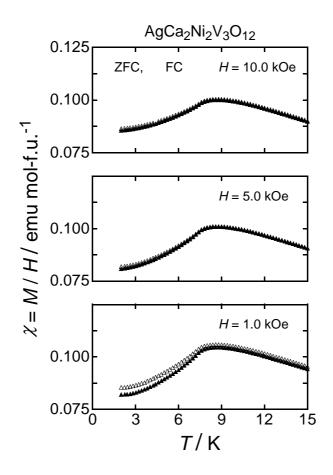


Fig. 20. Magnetic susceptibility of  $AgCa_2Ni_2V_3O_{12}$  as a function of temperature in three magnetic fields of 10.000 kOe, 5.000 kOe and 1.000 kOe under ZFC and FC conditions.

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