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Physical review. Third series. B, Condensed matter and materials physics

Volume 70
Number 22
Page range 220402-1-220402-4
Year 2004-12
URL http://hdl.handle.net/10258/212
DOI info:doi/10.1103/PhysRevB.70.220402
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Evidence for an antiferroquadrupolar ordering in YbSb probed by \(^{121}\)Sb and \(^{123}\)Sb nuclear magnetic resonances

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(Received 16 June 2004; published 3 December 2004)

Formation of the antiferroquadrupolar (AFQ) ordering in YbSb (NaCl-type structure) was evidenced microscopically with the \(^{121}\)Sb and \(^{123}\)Sb nuclear magnetic resonance (NMR) measurements. We have observed in the NMR linewidth below \(T_Q=5\) K the appearance of an additional field-independent contribution that is proportional to the nuclear electric-quadrupole moment. Thus, the field-independent contribution can be addressed not to any long-range magnetic orderings but to a broken symmetry of the charge distribution associated with the AFQ ordering. The AFQ ordering also gives rise to a large anisotropic Knight shift broadening caused by the anisotropy in the transferred hyperfine field and/or magnetic susceptibility. Fluctuations of the Yb 4f moments are also investigated by using the \(^{121,123}\)Sb spin-lattice relaxation rate measurements.

DOI: 10.1103/PhysRevB.70.220402
PACS number(s): 76.60.–k, 71.27.+a

Long-range ordering involving orbital degrees of freedom in transition-metal and rare-earth compounds is at the forefront of physics of the strongly correlated electron system. In contrast to transition-metal ions, lanthanide ions are characterized by the strong coupling between the total spin and orbital momenta, which rules out the pure orbital ordering. When the orbital degeneracy is not quenched out, however, it has been known that interactions between multipole (especially quadrupole) moments of the \(f\)-electron wave functions play a significant role on low-temperature physical properties, \(^1\) and even lead to a long-range ordered state \(^2\) in such as Ce and U compounds. \(^3,4\)

Low-carrier heavy-fermion ytterbium-monopnictides YbX (X=N,P,As,Sb) with a NaCl-type crystal structure have attracted much interest because of their unusual properties originating from the competition between the Kondo hybridization and the Ruderman-Kittel-Kasuya-Yosida (RKKY) interactions. \(^5\) Neutron diffraction and Mössbauer measurements showed that YbN, YbP, and YbAs have similar magnetic properties: antiferromagnetic (AFM) ordering with almost the same transition temperatures of about 0.5 K, and magnetic moments of about half of \(1.33\mu_B\) expected for the crystalline electric field (CEF) ground state \(\Gamma_6^0\). \(^6,7\)

For YbSb, on the other hand, Mössbauer, \(^8\) specific heat, \(^9\) and nuclear magnetic resonance (NMR) \(^10,11\) measurements reported the presence of two distinct phase transitions of the AFM ordering at 0.32 K and a possible antiferroquadrupolar (AFQ) ordering at 5 K. The CEF ground state of the \(\Gamma_6^0\) Kramers doublet has no quadrupole moment. Hashi et al. \(^5\) discussed the phase transition at 5 K in terms of a mixing-type AFQ ordering model \(^12\) with interactions between the ground state \(\Gamma_6^0\) and excited state \(\Gamma_q^e\) of Yb\(^{3+}\) ions. However, the phase transition at 5 K has been less studied experimentally and is not yet well established. In this study, we have performed \(^{121}\)Sb and \(^{123}\)Sb-NMR measurements to elucidate the phase transition microscopically.

A stoichiometric polycrystalline sample of YbSb was prepared with a wedgetype cubic-anvil high-pressure apparatus. X-ray powder diffraction measurements showed that the crystal structure is of NaCl type. The NMR measurement was carried out using a wideband phase-coherent spin-echo spectrometer in a temperature range between 1.4 and 100 K. NMR spectra of \(^{121}\)Sb (gyromagnetic ratio \(\gamma_s=1.0189\) kHz/Oe, nuclear spin \(I=\frac{5}{2}\), electric quadrupole moment \(Q=0.53\) b) and \(^{123}\)Sb (\(\gamma_s=0.55175\) kHz/Oe, \(I=\frac{7}{2}\), \(Q=-0.68\) b) were obtained in a field sweeping procedure at several constant frequencies in a range between 3.5 and 75 MHz. Above ~5 K, \(^{121,123}\)Sb-NMR spectra have a Lorentzian-type line shape, as shown in the inset of Fig. 1. The full width of half maximum (FWHM) is independent of temperature. Lack of any quadrupole splittings (or broadenings) is consistent with the cubic symmetry distribution of

![FIG. 1. Knight shift of \(^{121}\)Sb-NMR in YbSb at 29.5 and 70.5 MHz plotted against temperature. Inset of the figure shows typical NMR spectra above and below 5 K.](https://example.com/fig1.png)
the ionic charge on the neighboring lattice sites. The Knight shift \( K = (H_0 - H_{res})/H_{res} \) determined at the peak intensity point is plotted in Fig. 1 against temperature. Below \( \sim 5 \, \text{K} \), on the other hand, the \(^{121,123}\text{Sb}\)-NMR lines are largely broadened and have an anisotropic line shape (inset of Fig. 1). The Knight shifts \( K_i \) deduced from the peak and \( K_i \) from the shoulder of the spectra obtained at 29.5 and 70.5 MHz are also plotted in Fig. 1.

We plot in Fig. 2 the FWHM data for each of \(^{121}\text{Sb}\) and \(^{123}\text{Sb}\) against applied magnetic field \( H \). The important feature is that the FWHM below \( \sim 5 \, \text{K} \) consists of a magnetic field-dependent term \( \Delta H_M \) and a field-independent term \( \Delta H_0 \): \( \Delta H(H) = \Delta H_M(H) + \Delta H_0 \), which is consistent with the \(^{121}\text{Sb}\)-NMR data reported previously by Hashi \textit{et al.} \(^{11}\)

Values of \( \Delta H_0 \) can be deduced by extrapolating the linear relationship between the FWHM and applied magnetic field to \( H = 0 \). The results are plotted in the inset of Fig. 3 as a function of temperature. The field-independent contribution \( \Delta H_0 \) to the linewidth suddenly appears below \( \sim 5 \, \text{K} \) and tends to saturate at lower temperatures. Hashi \textit{et al.} suggested that the appearance of \( \Delta H_0 \) originates from a magnetic ordering of the Yb moments. \(^{11}\) However, we observed an isotope effect on the \(^{121}\text{Sb}\)- and \(^{123}\text{Sb}\)-NMR linewidths that does not support this conjecture.

As shown in Fig. 2, \( \Delta H_0 \) for \(^{123}\text{Sb}\) is larger than that for \(^{121}\text{Sb}\), and the isotope ratio \( \Delta H_0(^{121}\text{Sb})/\Delta H_0(^{123}\text{Sb}) = 0.63 \) is near to the nuclear quadrupole moment ratio \( Q(^{121}\text{Sb})/Q(^{123}\text{Sb}) = 0.78 \). Thus we conclude that the field-independent linewidth appeared below \( \sim 5 \, \text{K} \) originates from the first-order perturbation on the Zeeman-split nuclear-spin levels by the nuclear-quadrupole interaction between the electric field gradient (EFG) at the Sb nuclei and the quadrupole moment \( Q \). A small \( \Delta H_0 \) of about \( 10^2 \, \text{Oe} \) leads the pure nuclear-quadrupole resonance to a very low frequency that is hard to observe. The saturating behaviors of \( \Delta H_M \) below \( \sim 5 \, \text{K} \) at low frequency (Fig. 3) can be scaled by that of \( \Delta H_0 \), indicating that both are dominated by a single-order parameter. The additional small increase in \( \Delta H_M \) below \( \sim 5 \, \text{K} \) observed at high frequency is considered to be a precursor of the AFM ordering at \( T_N = 0.32 \, \text{K} \). It is worth noting that the value \( \Delta H_M \) is directly proportional to the applied magnetic field. This also indicates that the large increase in \( \Delta H_M \) below \( \sim 5 \, \text{K} \) is not caused by any long-range magnetic orderings of the Yb moments.

In a cubic crystal structure, the CEF Hamiltonian is expressed as\(^{15}\)

\[
\mathcal{H}_{CEF} = N[B_0^2(O_0^4 + 5O_6^4) + B_6^4(O_6^6 - 21O_8^6)],
\]

where \( B_i \) are CEF parameters and \( O_m^p \) are Steven’s operators. The \( J = \frac{5}{2} \) multiplet of \(^{121}\text{Sb}^+\) ion in YbX splits into a ground-state \( \Gamma_6 \) doublet, and two excited states of \( \Gamma_8 \) quartet and \( \Gamma_7 \) doublet.\(^{8,10,14}\) The spin degeneracy of the \( \Gamma_8 \) state is considered to be quenched out by the AFM ordering at \( 0.32 \, \text{K} \). The quadrupolar interaction \( H_{Q\ell} \) is given by the squared matrix element,

\[
q_{\ell\ell'} = \Sigma |\langle \ell | \gamma | \ell' \rangle |^2,
\]

of the \( \Gamma_\ell \)-type quadrupolar operators,\(^9\)

\[
u = J^2 - 2J(J+1),
\]

\[
\gamma = (J^2 - J^2)\sqrt{3},
\]

where \( \gamma \) denotes the components of \( \Gamma_\ell \). Within the \( \Gamma_6 \) doublet, there is no squared matrix element: \( q_{00} = 0 \). The largest element is a mixing-type coupling between the \( \Gamma_6 \) and \( \Gamma_8 \) states, \( q_{68} = q_{86} = 70 \), which can lead to a quadrupole ordering at low temperatures. The AFQ ordering can, therefore, be caused by the mixing-type coupling between the \( \Gamma_6 \) and \( \Gamma_8 \) states representing the asphericity of the charge distribution. The appearance of the nuclear-quadrupole broadening \( \Delta H_0 \) below \( \sim 5 \, \text{K} \) in the \(^{121,123}\text{Sb}\)-NMR spectra and, therefore, the EFG at the Sb site can be caused by this AFQ ordering with a different periodicity from that of the lattice.

At high temperatures above \( \sim 5 \, \text{K} \), the Knight shift of \(^{121}\text{Sb}\) is nearly isotropic. The negative value increases with decreasing temperature and takes a maximum near \( 5 \, \text{K} \) (Fig. 1). Below \( \sim 5 \, \text{K} \), the \(^{121}\text{Sb}\)-NMR spectrum becomes largely anisotropic in shape, and both \( K_i \) and \( K_i \) turn to decrease with decreasing temperature. Figure 4 shows the dependence of the \(^{121}\text{Sb}\)-Knight shift \( K \) on the uniform susceptibility \( \chi \) observed at \( 50 \, \text{kOe} \) (shown in the inset). This plot is motivated by the usual expression,
$K = (\gamma_n \gamma_r h^2)^{-1} A_{hf}/\chi$, where $A_{hf}/\gamma_r h$ is the hyperfine field on the observed nucleus.\textsuperscript{15} The slope of a straight-line relationship (solid line) obtained above $\sim 20$ K gives $A_{hf}/\gamma_r h = -10.3$ kOe/$\mu_B$ which is considered to be dominated by the transferred coupling with the Yb$^{3+}$ spins. Below $\sim 20$ K, the negative shift is smaller than would be predicted from linear extrapolation of the high-temperature data, indicating that the value of $A_{hf}$ decreases with decreasing temperature. The variation of $A_{hf}$ below $\sim 20$ K is expected if the hyperfine field is anisotropic, since then the $\Gamma_6$ ground-state wave function of the Yb$^{3+}$ ion will cause it to couple differently to neighboring Sb nuclei than the $\Gamma_8$ excited state.\textsuperscript{16,17} We note that $A_{hf}^0 < A_{hf}$ for the experimental decrease in $A_{hf}$ at low temperatures.

As can be seen in the inset of Fig. 2, the uniform susceptibility shows the monotonic increase down to 2 K, indicating that there is no long-range magnetic ordering. On the other hand, we found that the $^{121}$Sb-NMR spectrum below $\sim 5$ K, shows the large anisotropic Knight shift broadening, in addition to the small nuclear-quadrupole broadening. Utilizing the relations $K_{iso} = \frac{1}{2}(K_x + 2K_z)$ and $K_{an} = \frac{1}{2}(K_x - K_z)$, we obtain the isotropic Knight shift $K_{iso} = -5.29\%$ and anisotropic Knight shift $K_{an} = -0.35\%$ at 1.5 K. $K_{an}$ originates from the anisotropy in $A_{hf}$ and/or $\chi$. The AFQ ordering of the Yb$^{3+}$ ions gives rise to the anisotropy in the hyperfine field. The strong coupling between the total spin and orbital moments is also expected to cause the anisotropic susceptibility. In the present case of powdered sample, however, we cannot discriminate between these two contributions.

The $^{121}$Sb spin-lattice relaxation time $T_1$ was measured at the peak intensity point of the spectrum, utilizing a radio frequency (rf) single-pulse saturation method. Above $\sim 5$ K, the magnetization recovery $M(t)$ at time $t$ after the saturation pulse displayed a single-exponential behavior, $M(\infty) - M(t) = M(\infty) e^{-t/T_1}$. This is expected for equally separated nuclear spin levels in energy by the Zeeman interaction. With lowering temperature below $\sim 5$ K, on the other hand, the magnetization recovery tends to show a multieponential behavior. For unequally separated nuclear spin levels by the nuclear-quadrupole interaction perturbation, the diagonalization of the rate equation gives a magnetization recovery behavior expressed as\textsuperscript{18}

$$M(\infty) - M(t) \approx a_1 e^{-t/T_1} + a_2 e^{-6t/T_1} + a_3 e^{-15t/T_1} + a_4 e^{-28t/T_1},$$

(4)

where the coefficients $a_i$ ($i = 1–3$ for $^{121}$Sb, and $1–4$ for $^{123}$Sb) depend on the initial saturation condition imposed on the nuclear spin levels, and $\Sigma a_i = 1$. The experimental recovery data can be reproduced satisfactorily with Eq. (4), where the value of $a_1$ decreases rapidly with decreasing temperature. The anisotropy in the hyperfine field and/or susceptibility would give rise to a distribution of the relaxation rate. However, because of the small perturbing rf field $H_1$ of $\approx 50$ Oe when compared with the separation in field between the peak and shoulder of the spectrum, this is not considered to largely affect the experimental recovery curve measured at the peak intensity point. The values of $(T_1 T)^{-1}$ for $^{121}$Sb obtained at 12.0, 29.5, and 70.5 MHz are plotted in Fig. 5 against temperature on a log-log scale.

The $(T_1 T)^{-1}$ data for $^{123}$Sb measured at 35.0 MHz are also plotted in the figure. The isotope ratio of the relaxation rate $(T_1 T)^{-1}(^{121}\text{Sb})/(T_1 T)^{-1}(^{123}\text{Sb}) \sim 4$ is close to the squared gyromagnetic ratio $\gamma_s(121\text{Sb})/\gamma_s(123\text{Sb}) = 3.41$. This is an indication that the relaxation of the Sb nuclear spins is dominated not by the quadrupole relaxation $(T_1^{-1})_Q$ but the magnetic relaxation $(T_1^{-1})_M$. On the other hand, Oyamada et al. recently reported that $(T_1^{-1})_Q$ becomes effective below 5 K with different temperature dependence from that of $(T_1^{-1})_M$, and ascribed it to the quadrupolar ordering.\textsuperscript{19} We think, however, their $T_1$ data are not convincing, and not consistent with the experimental fact that magnetic linewidth $\Delta H_M$ below $\sim 5$ K at low frequency can be scaled by that of quadrupole linewidth $\Delta H_Q$. The different temperature dependence of $^{121}$Sb and $^{123}$Sb around 5 K could originate from different initial saturation conditions for the $T_1$ measurements.

As shown in Fig. 5, $(T_1 T)^{-1}$ is rather insensitive to the magnetic field, and increases with decreasing temperature without displaying any significant change near 5 K, as in the
increasing rate of prototypical quadrupolar ordering compound CeB$_6^{20}$ $(T_1T)^{-1}$ originates from the spin fluctuations is given by

$$(T_1T)^{-1} = \frac{k_B\gamma_s}{\mu_B^2} \sum_q A_{hf}(q)^2 \text{Im} \chi(q,\omega_0)/\omega_0,$$  \hspace{1cm} (5)

where $\chi(q,\omega)$ is the dynamical susceptibility, $q$ the wave vector of spin fluctuations, and $\omega_0$ the NMR frequency. The increasing rate of $(T_1T)^{-1}$ with decreasing temperature is larger than that of the uniform susceptibility $\chi(0,0)$ (inset of Fig. 4). Taking the decrease in $A_{hf}$ at low temperatures into account, this suggests that the staggered susceptibility $\chi(Q_{AF},0)$ originating from the 4f moments largely increases with decreasing temperature, which is consistent with the formation of the AFQ ordering with $q=Q_{AF}$. The fluctuation behavior of the Yb$^{3+}$ moments in the AFQ ordered state is quite interesting and calls for further detailed $T_1$ measurement.

The authors wish to express their thanks to Professor H. Shiba, Kobe University, for his valuable discussions. They also wish to acknowledge the support of Professor S. Nasu, Osaka University, in measuring the susceptibility of YbSb. This work was partially supported by a Grant-in-Aid for Scientific Research from the Ministry of Education, Science and Culture of Japan, Grant No. 16340105.

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