Single Radial/Azimuthal Mode Photonic Crystal Fibers With Anisotropic Elliptical-Hole Lattice Core

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Single Radial/Azimuthal Mode Photonic Crystal Fibers With Anisotropic Elliptical-Hole Lattice Core

Zheng Zhong, Student Member, IEEE, Yasuhide Tsuji, Member, IEEE, and Masashi Eguchi, Member, IEEE

Abstract—Novel single radial/azimuthal mode photonic crystal fibers (PCFs) with an anisotropic elliptical-hole lattice core (EHLC) are proposed and demonstrated numerically. High birefringence is achieved by introducing elliptical holes into the core, which is considered as an effective way to break the symmetry. With a full vectorial finite element method, we can optimize the fiber parameters and also investigate the wave guiding characteristics in detail. A bandwidth of 210 nm (the wavelength range from 1.45 to 1.66 μm) has been achieved for single radial mode transmission by the PCF with an actinomorphic EHLC. Meanwhile, a bandwidth of 100 nm (the wavelength range from 1.50 to 1.60 μm) for single azimuthal mode transmission has been also achieved by the PCF with a multi-annulus EHLC. It is anticipated that the proposed PCFs would be of very much convenience in mode multiplexing systems.

Index Terms—Photonic crystal fiber, single radial/azimuthal mode transmission, elliptical-hole lattice, finite element method.

I. INTRODUCTION

Single mode fibers (SMFs) play an important role for mode multiplexing in optical communication systems in recent years. SMFs can be classified into several types by the guidance mechanisms, such as conventional SMFs based on the total internal reflection [1], Bragg fibers based on the effect of Bragg reflection [2]-[4], and photonic crystal fibers (PCFs) based on the concept of photonic crystals [5], [6]. Due to the flexible structures and unique properties of PCFs, a lot of attentions have been paid on their research and development. One of the important parameters of PCFs is the birefringence, and there are two main methods to achieve a high birefringence. One is by introducing elliptical holes or other asymmetric air holes into the core [7]-[10], since elliptical holes are effective to break the symmetry [8]. The other is to change the refractive index contrast between the core and cladding by doping a liquid crystal in the core [12] or utilizing other materials such as metal, polymer, plastic, and so on. Due to the high birefringence, lots of single-polarization (single x- or y-polarization) single-mode (single HE_{11} mode) fibers have been demonstrated earlier. However, a single radial or azimuthal mode fiber has never been investigated by the PCFs so far.

In this letter, to our knowledge, we firstly propose the novel single radial/azimuthal mode PCFs, which have an anisotropic elliptical-hole lattice core (EHLC). First, we put forward an analysis to confirm that how much of the birefringence can support the single radial mode transmission based on an equivalent step-index (SI) fiber model in Section II. Next, we investigate the performances of the single radial mode PCF and single azimuthal mode PCF by employing the full vectorial finite element method (FV-FEM) [13] in Sections III and IV, respectively. Finally, we give a brief conclusion of all analyses in Section V.

II. EQUIVALENT STEP INDEX-FIBER MODEL

For convenience, we consider an equivalent model based on a 2-layer SI-fiber with a radius a of the core, which is shown in Fig. 1. In order to earn a birefringence B, we assume an anisotropic material in the core, whose refractive indices along longitudinal, radial, and azimuthal directions are defined as n_{1,z} = n_0, n_{1,r} = n_0 + B/2, and n_{1,θ} = n_0 - B/2, respectively. The cladding is characterized by an isotropic material, whose refractive index is defined as n_2 = n_0, where n_0 is assumed to be 1.444. At first, we discuss the dispersion of Δn_{eff} as a function of core radius a. Considering a high birefringence of 0.08 obtained in elliptical-hole holey fiber [14], B is changed from 0.02 to 0.10 with an interval of 0.02 and the operating wavelength is set to λ = 1.55 μm. Δn_{eff} stands for the difference of the modal effective refractive indices between the radial and HE_{11} modes, that can be expressed as the following equation:

\[ \Delta n_{eff} = n_{eff}^{Radial} - n_{eff}^{HE_{11}}, \]  

where n_{eff}^{Radial} and n_{eff}^{HE_{11}} indicate the modal effective refractive indices of radial and HE_{11} modes, respectively. It can be observed in Fig. 2 that, Δn_{eff} reaches to the maximum of 2.647 × 10^{-3} under the conditions of a = 3.5 μm and...
B = 0.10. Moreover, $\Delta n_{\text{eff}}$ decreases with an increase in the core radius. In order to achieve the single radial mode transmission, we need to adjust the refractive index of cladding. Fig. 3 shows the modal effective indices of radial and HE$_{11}$ modes with respect to the refractive index of cladding $n_2$. When the effective index equals the cladding index, the mode is in cutoff state, and thus we refer to the line with black dots corresponding to the cladding index as cutoff limit. The line with blue-colored open circles and the line with red-colored dashed circles indicate the modal effective indices of radial and HE$_{11}$ modes, respectively. We can observe that HE$_{11}$ mode crosses with the cutoff limit first at $n_2 = 1.480$, and then the radial mode crosses at $n_2 = 1.484$. Therefore, at the refractive index range from 1.480 to 1.484, the single radial mode transmission can be achieved in the equivalent SI-fiber. The magnetic field distributions and Poynting vectors of radial and HE$_{11}$ modes for $n_2 = 1.482$ are shown in Fig. 4. It can be observed that, the HE$_{11}$ mode is not guided and only the radial mode is confined in the core. That means that the single mode transmission can be achieved by the anisotropy between the radial and azimuthal directions of the core in the equivalent SI-fiber. Furthermore, The modal effective indices of radial and HE$_{11}$ modes and the cladding index as a function of wavelength is shown in Fig. 5. The light blue shaded region represents the non-confinement region, where the modal effective indices of radial (blue line) and HE$_{11}$ modes (red dashed line) are lower than that of the cladding index (dot line). In the wavelength range from 1.48 to 1.68 $\mu$m, the single radial mode transmission is achieved in the equivalent SI-fiber.

### III. SINGLE RADIAL MODE PHOTONIC CRYSTAL FIBER

On the basis of the equivalent SI-fiber model described in Section II, we propose a novel single radial mode PCF with an actinomorphic EHLIC to achieve the single radial mode transmission. Fig. 6 shows the schematic of the proposed PCF and the rough mesh division of a quarter cross-section. As shown in Fig. 6 (a), the proposed PCF is characterized by the fused-silica (SiO$_2$) with defected air holes in a triangular lattice. The centers of all air holes are arranged by the lattice pitch of $\Lambda$. The core is arranged by elliptical holes with the radii $R_L$ and $R_S$ for the major and minor axes, respectively. With these major axes of elliptical holes along the radial directions and a large circular hole with a radius of $R_a$ in the center, the radial mode will be guided more easily than the HE$_{11}$ mode. The radius of cladding air hole is represented by $R_c$. Considering the material dispersion of SiO$_2$ existing in the real applications, we calculate the refractive index of fused-silica based on the Sellmeier equation [15], which is expressed as follows:

$$n^2(\lambda) = 1 + \frac{0.6961663\lambda^2}{\lambda^2 - (0.0684043)^2} + \frac{0.4079426\lambda^2}{\lambda^2 - (0.1162414)^2} + \frac{0.8974794\lambda^2}{\lambda^2 - (9.8961610)^2}. \quad (2)$$

The refractive index of air is set to 1.0. Due to the structural symmetries along the x- and y-axes, we can only calculate a quarter cross-section to reduce the analysis cost. In Fig. 6 (b), a rough mesh division of a quarter cross-section of the PCF is shown, where the symmetric boundary conditions (Γ$_1$, Γ$_2$) and (Γ$_3$ and Γ$_4$) are loaded by the perfect magnetic conductor (PMC) and the perfect electric conductor (PEC), respectively, for the single radial mode PCF analyses. For more accurate
analyses, we give the rough quarter mesh another 50,000 divisions. After that, we select $\Lambda = 1 \mu m$, $R_a = 0.40\Lambda$, $R_S = 0.24\Lambda$, and $R_L = 2R_S$ as the optimizing parameters to earn the highest birefringence. First, we set $R_c = \sqrt{2R_S^2}$, which makes both areas of an elliptical hole and an air hole in the cladding equal. In other words, we approximate that the modal effective indices of core and cladding are the same to guide the radial and HE$_{11}$ modes, simultaneously. Fig. 7 shows the relation between the modal effective index difference $\Delta n_{eff}^R = n_{eff}^{Radial} - n_{eff}^{HE_{11}}$ and the number of core rings with respect to wavelength. At the communication wavelength of 1.55 $\mu m$, the maximum of $\Delta n_{eff}^R$ reaches $1.591 \times 10^{-3}$ with a 5-ring core. Next, we select an optimal size of $R_c$ to achieve the single radial mode transmission in the proposed PCF. when $R_c = 0.322\Lambda$, the bandwidth of single radial mode transmission is the widest. In the wavelength range from 1.45 to 1.66 $\mu m$ (a bandwidth of 210 nm), the single radial mode transmission is achieved in the proposed PCF with an actinomorphic EHLC. At that time, the magnetic field distributions of both modes are shown in Fig. 8 at a wavelength of 1.55 $\mu m$. The single radial mode is confined, while the HE$_{11}$ mode is not guided. Table I represents the single mode bandwidth (SMB) and its wavelength range (WR) of the proposed PCF, when the elliptical and cladding holes are deviated within $\pm 0.3\%$. when elliptical holes become large (represented by “+”), the single radial mode band shifts toward longer wavelength and the bandwidth is slightly expanded. When they become small (represented by “−”), the band shifts toward to shorter wavelength. On the contrary, the circumstance of cladding holes represents the opposite trend. All the analyses are employed by the FV-FEM with curvilinear hybrid edge/nodal elements, the analyzed region is about $18.0 \times 15.6 \mu m^2$, and the total unknowns are 295,550 in the single radial mode PCF analyses.

IV. SINGLE AZIMUTHAL MODE PHOTONIC CRYSTAL FIBER

Based on the discussions in Sections II and III, we consider the schematic of a single azimuthal mode PCF with a multi-annulus EHLC as shown in Fig. 9, which is formed by rotating the elliptical holes in the core of Fig. 6 by 90°. As same as the circumstance in the single radial mode PCF analyses, only a quarter cross-section is calculated, and symmetric boundary conditions ($\Gamma'_1$, $\Gamma'_2$) and ($\Gamma'_3$, $\Gamma'_4$) are loaded by PEC and PMC, respectively, which is shown in Fig. 9 (b). After rotating, the SiO$_2$ area around the large circular hole gets increased. Fig. 10 shows the modal effective indices of two modes and its difference $\Delta n_{eff}^A = n_{eff}^{Azimuthal} - n_{eff}^{HE_{11}}$ as functions of the radius of large circular hole $R_a$. Here the radius of cladding air hole is set to $R_c = \sqrt{2R_S}$. It can be observed that, with the increasing $R_a$, the effective index of azimuthal mode is almost flat, conversely, the effective index of HE$_{11}$ mode declines. When $R_a = 0.49\Lambda$, $\Delta n_{eff}^A$ reaches the maximum of $1.205 \times 10^{-3}$. On the condition, when we select $R_c = 0.3235\Lambda$, the single azimuthal mode transmission is achieved in the wavelength range from 1.50 to 1.60 $\mu m$, and the bandwidth of that is 100 nm. Fig. 11 shows the magnetic field distributions of both modes at a wavelength of 1.55 $\mu m$. We can observe that the single azimuthal mode has an orthogonal relation with the single radial mode. And the FEM computational window is set to be the same as that in the single radial mode PCF analyses in the previous Section, except that the total unknowns are 295,854 in the single azimuthal mode PCF analyses. Table II represents the single azimuthal mode bandwidth and its wavelength range of the proposed PCF, when the elliptical and cladding holes are deviated only in $\pm 0.1\%$. The phenomenon of the band shift is as same as that in the single radial mode PCF. With a minor change of the air holes, the single azimuthal mode transmission is hardly achieved in the wavelength of 1.55 $\mu m$ in

![Fig. 6. The schematic of the proposed single radial mode PCF with an actinomorphic EHLC (a), and the rough mesh division of a quarter cross-section (b), where the symmetric boundaries ($\Gamma'_1$, $\Gamma'_2$) and ($\Gamma'_3$, $\Gamma'_4$) are loaded by PMC and PEC, respectively.](image)

![Fig. 7. The modal effective index difference $\Delta n_{eff}^R$ in different core rings as a function of wavelength.](image)

![Fig. 8. The magnetic field distributions ($H_x$ and $H_y$) of both modes in the proposed single radial mode PCF, at $\lambda = 1.55 \mu m$.](image)

![Table I: Single azimuthal mode bandwidth and its wavelength range versus the deviation level of elliptical and cladding holes](image)
the proposed PCF with a multi-annulus EHLC. The presented results have been estimated for uniform structural fluctuations. So, the presented tolerances are the worst estimations. In fact, the random structural fluctuations may be somewhat canceled out each other for the wavelength range deviations.

V. CONCLUSION

The single radial/azimuthal mode transmission has been numerically demonstrated by the proposed PCFs with an anisotropic EHLC. The analyses based on the equivalent SI-fiber model give the theoretical criteria for designing the proposed PCFs. The bandwidths of 210 nm for the single radial mode transmission and 100 nm for the single azimuthal mode transmission have been achieved in the PCFs with an actinomorphic EHLC and with a multi-annulus EHLC, respectively. Although, the precision problem in fabricating elliptical holes does exist, the research and development of the fabrication techniques are in high progress. Combined with the existing techniques such as the stack and draw technique [16], post-processing technique, flame brushing technique, interleaved stacking technique and so on [17], the fabrication of elliptical holes will not be the most critical problem in the applications. Although the operating wavelength of the EHLC proposed here is sensitive to structural deviation, we would like to discuss more insensitive structures in the future work. Based on this, we believe that the proposed PCFs will be a significant advance for the mode multiplexing in optical communication systems.

REFERENCES